

QUESTION

$$r_n = 3^n (A + Bn)$$

$$r_{n+2} - 6r_{n+1} + 9r_n = 0$$

First we find $r_{n+2} = ?$

So,

$$r_{n+2} = 3^{n+2} (A + Bn+2)$$

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Now, $6r_{n+1} = ?$

$$6r_{n+1} = 6 \{ 3^{n+1} (A + Bn+1) \}$$

$$= 18^{n+1} (6A + 6Bn+1)$$

Now, $9r_n = ?$

$$9r_n = 9 \{ 3^n (A + Bn) \}$$

$$= 27^n (9A + 9Bn)$$

So,

$$= 3^{n+2} (A + Bn+2) - 18^{n+1} (6A + 6Bn+1)$$

$$+ 27^n (9A + 9Bn)$$

$$= 3^{n+2} A + 3^{n+2} Bn+2 - 108^{n+1} A - 108^{n+1} Bn+1$$

$$+ 243A + 243Bn$$

$$= 3^{n+2} A - 108^{n+1} A + 243A + 3^{n+2} Bn+2$$